

(30)

Factoring Quadratic Expressions - X-Method

Factoring in the form of $\cdot ax^2 + bx + c$.

$$\frac{1}{a}x^2 + \frac{12}{b}x + \frac{35}{c}$$

Steps:

- 1) Draw an "X" next to the problem.
- 2) Multiply " $a \cdot c$ " and place at the top of the "X".
$$\begin{array}{c} 35 \\ \times 5 \\ \hline 175 \end{array}$$
- 3) Place " b " at the bottom of the "X".
$$\begin{array}{c} 35 \\ \times 5 \\ \hline 12 \end{array}$$
- 4) Find two numbers that multiply to give " $a \cdot c$ " and add to give " b ".
$$(x+5)(x+7)$$

Use the "table" button in the calculator,
"Edit Function" and insert " $a \cdot c / x$ " as the equation
and "start" at "1". This will give you all the factor pairs.
- 5) Make a list of the factors and decide on the signs.
- 6) Write your factors in each set of parenthesis.

EX) $x^2 + 10x + 24$

a) 1

b) 10

c) 24

24

4

6

$$(x+4)(x+6)$$

$$(x+8)(x+3)$$

EX) $x^2 - 2x - 15$

a) 1

b) -2

c) -15

124

212

38

46

$$(x+3)(x-5)$$

$$(x+8)(x-3)$$

-15

3-5

-2

15

35

Ex) $5x^2 - 10x - 400$ * GCF alert

$$\begin{array}{r} 5 \\ \overline{)5x^2 - 10x - 400} \\ \underline{-5} \\ \hline x^2 - 2x - 80 \end{array}$$

$$5(x^2 - 2x - 80)$$

a) 1

b) -2 $5(x+8)(x-10)$

c) -80

$$\begin{array}{r} 1 - 80 \\ -80 \\ \hline \end{array}$$

$$\begin{array}{r} 1 - 80 \\ 2 - 40 \\ \hline \end{array}$$

$$\begin{array}{r} 1 - 80 \\ 2 - 40 \\ 4 - 20 \\ \hline \end{array}$$

$$\begin{array}{r} 1 - 80 \\ 2 - 40 \\ 4 - 20 \\ 5 - 10 \\ \hline \end{array}$$

$$\begin{array}{r} 1 - 80 \\ 2 - 40 \\ 4 - 20 \\ 5 - 10 \\ 8 - 10 \\ \hline \end{array}$$

What happens when "a" > 1

- Follow steps 1-5.

- After the factor pair is chosen, divide

- simplify by the value of "a".

- Then complete the parenthesis. Fractions

- are not allowed, so kick the denominator to the front of the variable. $(x + \frac{3}{2})(2x + 3)$

Ex) $2x^2 - 13x + 15$ 2.15

a) 2

b) -13

c) 15

$$(x - \frac{3}{2})(x - 5)$$

$$(2x - 3)(x - 5)$$

$$\begin{array}{r} 30 \\ -3 \\ \hline 2 \\ -13 \\ \hline -10 \\ 2 \\ \hline -5 \\ 2 \\ \hline -6 \\ \hline \end{array}$$

$$\begin{array}{r} 1 - 30 \\ -2 - 15 \\ \hline 3 - 10 \\ \hline \end{array}$$

$$\begin{array}{r} 1 - 30 \\ -2 - 15 \\ 3 - 10 \\ \hline 5 - 6 \\ \hline \end{array}$$

Ex) $\frac{10x^2 + 6x - 36}{2}$

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